COLLEGE
ALGEBRA

## Enhanced with Graphing Utilities

Seventh Edition


## Available in MyMathLab ${ }^{\circledR}$ for Your College Algebra Course



## Achieve Your Potential

Success in math can make a difference in your life. MyMathLab is a learning experience with resources to help you achieve your potential in this course and beyond. MyMathLab will help you learn the new skills required, and also help you learn the concepts and make connections for future courses and careers.

## Visualization and Conceptual Understanding

These MyMathLab resources will help you think visually and connect the concepts.

## NEW! Guided Visualizations

These engaging interactive figures bring mathematical concepts to life, helping students visualize the concepts through directed explorations and purposeful manipulation. Guided Visualizations are assignable in MyMathLab and encourage active learning, critical thinking, and conceptual learning.


## EXAMPLE

Finding Vertical Asymptotes
Find the vertical asymptotes, if any, of the graph of exch rational fuection.

$$
\begin{aligned}
& R(x)=\frac{5 x^{2}}{3+x} \\
& R(x)=\frac{x^{2}-3 x-4}{x^{2}+x+1}=\frac{(x-4)(x+1)}{x^{2}+x+1} \\
& x^{2}+x+1=0
\end{aligned}
$$

## Video Assessment Exercises

Video assessment is tied to key Author in Action videos to check students' conceptual understanding of important math concepts. Students watch a video and work corresponding assessment questions.

## Preparedness and Study Skills

MyMathLab ${ }^{\circledR}$ gives access to many learning resources that refresh knowledge of topics previously learned. Getting Ready material, Retain Your Knowledge Exercises, and Note-Taking Guides are some of the tools available.


## Getting Ready

Students refresh prerequisite topics through skill review quizzes and personalized homework integrated in MyMathLab. With Getting Ready content in MyMathLab students get just the help they need to be prepared to learn the new material.

## Retain Your Knowledge Exercises

New! Retain Your Knowledge Exercises support ongoing review at the course level and help students maintain essential skills.


## Guided Lecture Notes

Get help focusing on important concepts with the use of this structured organized note-taking tool. The Guided Lecture Notes are available in MyMathLab for download or as a printed student supplement.

## BREAK THKTOUGH

To improving results

## Get the most out of MyMathLab ${ }^{\circledR}$

MyMathLab, Pearson's online learning management system, creates personalized experiences for students and provides powerful tools for instructors. With a wealth of tested and proven resources, each course can be tailored to fit your specific needs. Talk to your Pearson Representative about ways to integrate MyMathLab into your course for the best results.


## Data-Driven Reporting for Instructors

- MyMathLab's comprehensive online gradebook automatically tracks students' results to tests, quizzes, homework, and work in the study plan.
- The Reporting Dashboard, found under More Gradebook Tools, makes it easier than ever to identify topics where students are struggling, or specific students who may need extra help.


## Learning in Any Environment

- Because classroom formats and student needs continually change and evolve, MyMathLab has built-in flexibility to accommodate various course designs and formats.
- With a new, streamlined, mobile-friendly design, students and instructors can access courses from
 most mobile devices to work on exercises and review completed assignments.


## Prepare for Class "Read the Book"

| Feature | Description | Benefit | Page(s) |
| :---: | :---: | :---: | :---: |
| Every Chapter Opener begins with ... |  |  |  |
| Chapter-Opening Topic \& Project | Each chapter begins with a discussion of a topic of current interest and ends with a related project. | In the concluding project, you will apply what you have learned to solve a problem related to the topic. | 407,511 |
| (ค) <br> Internet-Based Projects | These projects allow for the integration of spreadsheet technology that you will need to be a productive member of the workforce. | The projects give you an opportunity to collaborate and use mathematics to deal with issues of current interest. | 407,511 |
| Every Section begins with ... |  |  |  |
| Learning Objectives $2$ | Each section begins with a list of objectives. Individual objectives also appear in the text where they are covered. | These objectives focus your studying by emphasizing what's most important and where to find it. | 428 |
| Sections contain ... |  |  |  |
| PREPARING FOR THIS SECTION | Most sections begin with a list of key concepts to review, with page numbers. | Ever forget what you've learned? This feature highlights previously learned material to be used in this section. Review it, and you'll always be prepared to move forward. | 428 |
| Now Work the 'Are You Prepared?' Problems | These problems assess whether you have the prerequisite knowledge for the upcoming section. | Not sure you need the Preparing for This Section review? Work the 'Are You Prepared?' problems. If you get one wrong, you'll know exactly what you need to review and where to review it! | 428,439 |
| Now Work <br> problems | These follow most examples and direct you to a related exercise. | We learn best by doing. You'll solidify your understanding of examples if you try a similar problem right away, to be sure you understand what you've just read. | 437 |
| WARNING | Warnings are provided in the text. | These point out common mistakes and help you avoid them. | 462 |
| Explorations and Seeing the Concept | These graphing utility activities foreshadow a concept or reinforce a concept just presented. | You will obtain a deeper and more intuitive understanding of theorems and definitions. | 377,434 |
| In Words | This feature provides alternative descriptions of select definitions and theorems. | Does math ever look foreign to you? This feature translates math into plain English. | 430 |
| $\widehat{A} \text { calculus }$ | This symbol appears next to information essential for the study of calculus. | Pay attention-if you spend extra time now, you'll do better later! | $\begin{array}{r} 236,238 \\ 373 \end{array}$ |
| SHOWCASE EXAMPLES | These examples provide "how to" instruction by offering a guided, step-by-step approach to solving a problem. | With each step presented on the left and the mathematics displayed on the right, you can immediately see how each step is employed. | 342-343 |
| Model It! Examples and Problems | These examples and problems require you to build a mathematical model from either a verbal description or data. The homework Model It! problems are marked by purple problem numbers. | It is rare for a problem to come in the form "Solve the following equation." Rather, the equation must be developed based on an explanation of the problem. These problems require you to develop models that will enable you to describe the problem mathematically and suggest a solution to the problem. | 453,482 |

## Practice "Work the Problems"

| Feature | Description | Benefit | Page(s) |
| :---: | :---: | :---: | :---: |
| 'Are You Prepared?' Problems | These problems assess your retention of the prerequisite material. Answers are given at the end of the section exercises. This feature is related to the Preparing for This Section feature. | Do you always remember what you've learned? Working these problems is the best way to find out. If you get one wrong, you'll know exactly what you need to review and where to review it! | 428, 439 |
| Concepts and Vocabulary | These short-answer questions, mainly fill-in-the-blank, multiple-choice, and true/false items, assess your understanding of key definitions and concepts in the current section. | It is difficult to learn math without knowing the language of mathematics. These problems test your understanding of the formulas and vocabulary. | 440 |
| Skill Building | Correlated with section examples, these problems provide straighfforward practice. | It's important to dig in and develop your skills. These problems give you ample opportunity to do so. | 440-442 |
| Mixed Practice | These problems offer comprehensive assessment of the skills learned in the section by asking problems related to more than one concept or objective. These problems may also require you to utilize skills learned in previous sections. | Learning mathematics is a building process. Many concepts build on each other and are related. These problems help you see how mathematics builds on itself and how the concepts are linked together. | 442 |
| Applications and Extensions | These problems allow you to apply your skills to real-world problems. They also enable you to extend concepts learned in the section. | You will see that the material learned within the section has many uses in everyday life. | 442-444 |
| Explaining Concepts: Discussion and Writing | "Discussion and Writing" problems are colored red. They support class discussion, verbalization of mathematical ideas, and writing and research projects. | To verbalize an idea, or to describe it clearly in writing, shows real understanding. These problems nurture that understanding. Many are challenging, but you'll get out what you put in. | 445 |
| NEW! <br> Retain Your Knowledge | These problems allow you to practice content learned earlier in the course. | Remembering how to solve all the different kinds of problems that you encounter throughout the course is difficult. This practice helps you remember previously learned skills. | 445 |
| Now Work <br> PROBLEMS | Many examples refer you to a related homework problem. These related problems are marked by a pencil and orange numbers. | If you get stuck while working problems, look for the closest Now Work problem, and refer to the related example to see if it helps. | $\begin{gathered} 429,437 \\ 438,441 \end{gathered}$ |
| Review Exercises | Every chapter concludes with a comprehensive list of exercises to practice. Use the list of objectives to determine what objective and examples correspond to each problem. | Work these problems to ensure that you understand all the skills and concepts employed in the chapter. Think of it as a comprehensive review of the chapter. All answers to Chapter Review problems appear in the back of the text. | 506-509 |

## Review "Study for Quizzes and Tests"

| Feature | Description | Benefit | Page(s) |
| :---: | :---: | :---: | :---: |
| The Chapter Review at the end of each chapter contains ... |  |  |  |
| Things to Know | A detailed list of important theorems, formulas, and definitions from the chapter. | Review these and you'll know the most important material in the chapter! | 504-505 |
| You Should Be Able to ... | A complete list of objectives by section and, for each, examples that illustrate the objective, and practice exercises that test your understanding of the objective. | Do the recommended exercises and you'll have mastered the key material. If you get something wrong, go back and work through the example listed, and try again. | 505-506 |
| Review Exercises | These provide comprehensive review and practice of key skills, matched to the Learning Objectives for each section. | Practice makes perfect. These problems combine exercises from all sections, giving you a comprehensive review in one place. | 506-509 |
| Chapter Test | About 15-20 problems that can be taken as a Chapter Test. Be sure to take the Chapter Test under test conditions-no notes! | Be prepared. Take the sample practice test under test conditions. This will get you ready for your instructor's test. If you get a problem wrong, you can watch the Chapter Test Prep Video. | 509 |
| Cumulative Review | These problem sets appear at the end of each chapter, beginning with Chapter 2. They combine problems from previous chapters, providing an ongoing cumulative review. When you use them in conjunction with the Retain Your Knowledge problems, you will be ready for the final exam. | These problem sets are really important. Completing them will ensure that you are not forgetting anything as you go. This will go a long way toward keeping you primed for the final exam. | 510 |
| Chapter Projects | The Chapter Projects apply to what you've learned in the chapter. Additional projects are available on the Instructor's Resource Center (IRC). | The Chapter Projects give you an opportunity to apply what you've learned in the chapter to the opening topic. If your instructor allows, these make excellent opportunities to work in a group, which is offen the best way of learning math. | 511 |
| (ค) <br> Internet-Based Projects | In selected chapters, a Web-based project is given. | These projects give you an opportunity to collaborate and use mathematics to deal with issues of current interest by using the Internet to research and collect data. | 511 |

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# COLLEGE ALGEBRA Enhanced with Graphing Utilities Seventh Edition 

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## PEARSON

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## In Memory of Mary... Wife and Mother

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## Three Distinct Series

Students have different goals, learning styles, and levels of preparation. Instructors have different teaching philosophies, styles, and techniques. Rather than write one series to fit all, the Sullivans have written three distinct series. All share the same goal-to develop a high level of mathematical understanding and an appreciation for the way mathematics can describe the world around us. The manner of reaching that goal, however, differs from series to series.

## Enhanced with Graphing Utilities Series, Seventh Edition

This series provides a thorough integration of graphing utilities into topics, allowing students to explore mathematical concepts and encounter ideas usually studied in later courses. Using technology, the approach to solving certain problems differs from the Contemporary or Concepts through Functions Series, while the emphasis on understanding concepts and building strong skills does not: College Algebra, Algebra \& Trigonometry, Precalculus.

## Contemporary Series, Tenth Edition

The Contemporary Series is the most traditional in approach, yet modern in its treatment of precalculus mathematics. Graphing utility coverage is optional and can be included or excluded at the discretion of the instructor: College Algebra, Algebra \& Trigonometry, Trigonometry: A Unit Circle Approach, Precalculus.

## Concepts through Functions Series, Third Edition

This series differs from the others, utilizing a functions approach that serves as the organizing principle tying concepts together. Functions are introduced early in various formats. This approach supports the Rule of Four, which states that functions are represented symbolically, numerically, graphically, and verbally. Each chapter introduces a new type of function and then develops all concepts pertaining to that particular function. The solutions of equations and inequalities, instead of being developed as stand-alone topics, are developed in the context of the underlying functions. Graphing utility coverage is optional and can be included or excluded at the discretion of the instructor: College Algebra; Precalculus, with a Unit Circle Approach to Trigonometry; Precalculus, with a Right Triangle Approach to Trigonometry.

