

Sixth Edition

# POWER SYSTEM ANALYSIS & DESIGN

J. Duncan Glover  
Thomas J. Overbye  
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# POWER SYSTEM ANALYSIS & DESIGN

SIXTH EDITION



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**Power System Analysis & Design,  
Sixth Edition**

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and Mulukutla S. Sarma

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Cover Image: High voltage power lines  
and pylon, kstudija/Shutterstock.com;  
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WCN: 02-200-203

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Library of Congress Control Number: 2015956452

ISBN: 978-1-305-63213-4

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Printed in the United States of America  
Print Number: 01      Print Year: 2015



In loving memory of my mentors Professor Fred C. Schweppe [1933–1988] and Dr. Alexander Kusko [1921–2013]. You taught me, you guided me, you set the bar for which I continue to strive. You shall not be forgotten.

### **My Guardian Poet[s]**

A guardian poet you have been to me  
Much like an angel, there protecting me  
When I was silent, lost in dark of night  
You read my words and brought me back to light

You told me that my words were ever true  
That in my writes were thoughts profound and new  
You would not let me simply drift away  
A word of hope you'd send to greet each day

Your name is there below each thing I write  
To tear dimmed eyes you brought a vision bright  
“The Queen of Passion,” how I love the name  
You gave to me and life is not the same

To you, my Guardian Poet, thanks I bring  
You fool me not; I see your angel wing

*Eileen Manassian Ghali*

To Jo, Tim, Hannah, and Amanda

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# Preface

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The objective of this book is to present methods of power system analysis and design, particularly with the aid of a personal computer, in sufficient depth to give the student the basic theory at the undergraduate level. The approach is designed to develop students' thinking processes, enabling them to reach a sound understanding of a broad range of topics related to power system engineering, while motivating their interest in the electrical power industry. Because we believe that fundamental physical concepts underlie creative engineering and form the most valuable and permanent part of an engineering education, we highlight physical concepts while giving due attention to mathematical techniques. Both theory and modeling are developed from simple beginnings so that they can be readily extended to new and complex situations.

## NEW TO THIS EDITION

New chapter-opening case studies bring principles to life for students by providing practical, real-world engineering applications for the material discussed in each chapter.

Comprehensively revised problem sets ensure students have the practice they need to master critical skills.

## Updated Instructor Resources

These resources include

- Instructor's Solutions Manual with solutions to all problems
- Comprehensive Test Bank offering additional problems
- Annotated Lecture Note PowerPoint Slides
- Lesson Plans that detail how to most effectively use this edition
- Updated PowerWorld Simulator Software
- Student PowerPoint Notes

New design projects in this edition meet Accreditation Board for Engineering and Technology (ABET) requirements to provide valuable hands-on experience and to help ensure students are receiving an education that meets globally recognized accreditation standards.

The latest version of the valuable PowerWorld Simulator (version 19) is included and integrated throughout the text.

## KEY FEATURES

The text presents present-day, practical applications and new technologies along with ample coverage of the ongoing restructuring of the electric utility industry. It is supported by an ample number of worked examples, including illustrations, covering most of the theoretical points raised. It also includes PowerWorld Simulator version 19 to extend fully worked examples into computer implementations of the solutions. Version 19 includes power flow, optimal power flow, contingency analysis, short circuit, and transient stability.

The text includes a chapter on Power Distribution with content on Smart Grids.

It also includes discussions on modeling of wind turbines in power flow and transient stability.

Four design projects are included, all of which meet ABET requirements.

## POWERWORLD SIMULATOR

One of the most challenging aspects of engineering education is giving students an intuitive feel for the systems they are studying. Engineering systems are, for the most part, complex. While paper-and-pencil exercises can be quite useful for highlighting the fundamentals, they often fall short in imparting the desired intuitive insight. To help provide this insight, the book uses PowerWorld Simulator version 19 to integrate computer-based examples, problems, and design projects throughout the text.

PowerWorld Simulator was originally developed at the University of Illinois at Urbana-Champaign to teach the basics of power systems to nontechnical people involved in the electricity industry, with version 1.0 introduced in June 1994. The program's interactive and graphical design made it an immediate hit as an educational tool, but a funny thing happened—its interactive and graphical design also appealed to engineers doing analysis of real power systems. To meet the needs of a growing group of users, PowerWorld Simulator was commercialized in 1996 by the formation of PowerWorld Corporation. Thus while retaining its appeal for education, over the years PowerWorld Simulator has evolved into a top-notch analysis package, able to handle power systems of any size. PowerWorld Simulator is now used throughout the power industry, with a range of users encompassing universities, utilities of all sizes, government regulators, power marketers, and consulting firms.

In integrating PowerWorld Simulator with the text, our design philosophy has been to use the software to extend, rather than replace, the fully worked examples provided in previous editions. Therefore, except when the problem size makes it impractical, each PowerWorld Simulator example includes a fully worked hand solution of the problem along with a PowerWorld Simulator case. This format allows students to simultaneously see the details of how a problem is solved and a computer implementation of the solution. The added benefit from PowerWorld Simulator is its ability to easily extend the example. Through its interactive design, students can quickly vary example parameters and immediately see the impact such changes have on the solution. By reworking the examples with the new parameters, students get immediate feedback on whether they understand the solution process.



The interactive and visual design of PowerWorld Simulator also makes it an excellent tool for instructors to use for in-class demonstrations. With numerous examples utilizing PowerWorld Simulator instructors can easily demonstrate many of the text topics. Additional PowerWorld Simulator functionality is introduced in the text problems and design projects.

## PREREQUISITES

As background for this course, it is assumed that students have had courses in electric network theory (including transient analysis) and ordinary differential equations and have been exposed to linear systems, matrix algebra, and computer programming. In addition, it would be helpful, but not necessary, to have had an electric machines course.

## ORGANIZATION

The text is intended to be fully covered in a two-semester or three-quarter course offered to seniors and first-year graduate students. The organization of chapters and individual sections is flexible enough to give the instructor sufficient latitude in choosing topics to cover, especially in a one-semester course. The text is supported by an ample number of worked examples covering most of the theoretical points raised. The many problems to be worked with a calculator as well as problems to be worked using a personal computer have been revised in this edition.

After an introduction to the history of electric power systems along with present and future trends, *Chapter 2* orients the students to the terminology and serves as a brief review of fundamentals. The chapter reviews phasor concepts, power, and single-phase as well as three-phase circuits.

*Chapters 3 through 5* examine power transformers including the per-unit system, transmission-line parameters, and steady-state operation of transmission lines. *Chapter 6* examines power flows including the Newton-Raphson method, power-flow modeling of wind generation, economic dispatch, and optimal power flow. These chapters provide a basic understanding of power systems under balanced three-phase, steady-state, normal operating conditions.

*Chapters 7 through 10*, which cover symmetrical faults, symmetrical components, unsymmetrical faults, and system protection, come under the general heading of power system short-circuit protection. *Chapter 11* examines transient stability, which includes the swing equation, the equal-area criterion, and multi-machine stability with modeling of wind-energy systems. *Chapter 12* covers power system controls, including generator-voltage control, turbine-governor control, and load-frequency control. *Chapter 13* examines transient operation of transmission lines including power system overvoltages and surge protection.

*Chapter 14* introduces the basic features of primary and secondary distribution systems as well as basic distribution components including distribution substation transformers, distribution transformers, and shunt capacitors. We list some of the major distribution software vendors followed by an introduction to distribution reliability, distribution automation, and smart grids.

## ADDITIONAL RESOURCES

Companion websites for this book are available for both students and instructors. These websites provide useful links and other support material.

### Student Website

The **Student Companion Site** includes a link to download the free student version of PowerWorld and Student PowerPoint Notes.

### Instructor Resource Center

The **Instructor Companion Site** includes

- Instructor's Solutions Manual
- Annotated PowerPoint Slides
- Lecture Notes
- Test Banks

To access the support material described here along with all additional course materials, please visit <https://sso.cengage.com>.

## MINDTAP ONLINE COURSE AND READER

This textbook is also available online through Cengage Learning's MindTap, a personalized learning program. Students who purchase the MindTap have access to the book's multimedia-rich electronic Reader and are able to complete homework and assessment material online, on their desktops, laptops, or iPads. Instructors who use a Learning Management System (such as Blackboard, Canvas, or Moodle) for tracking course content, assignments, and grading, can seamlessly access the MindTap suite of content and assessments for this course.

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- Personalize the Learning Path to match the course syllabus by rearranging content or appending original material to the online content
- Connect a Learning Management System portal to the online course and Reader
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Additionally, students can listen to the text through ReadSpeaker, take notes in the digital Reader, study from and create their own Flashcards, highlight content for easy reference, and check their understanding of the material through practice quizzes and automatically-graded homework.

## ACKNOWLEDGMENTS

The material in this text was gradually developed to meet the needs of classes taught at universities in the United States and abroad over the past 35 years. The original 13 chapters were written by the first author, J. Duncan Glover, *Failure Electrical LLC*,

who is indebted to many people who helped during the planning and writing of this book. The profound influence of earlier texts written on power systems, particularly by W. D. Stevenson, Jr., and the developments made by various outstanding engineers are gratefully acknowledged. Details of sources can only be made through references at the end of each chapter, as they are otherwise too numerous to mention.

Chapter 14 (*Power Distribution*) was a collaborative effort between Dr. Glover (Sections 14.1-14.7) and Co-author Thomas J. Overbye (Sections 14.8 & 14.9). Professor Overbye, *University of Illinois at Urbana-Champaign* updated Chapter 6 (*Power Flows*) and Chapter 11 (*Transient Stability*). He also provided the examples and problems using PowerWorld Simulator as well as three design projects. Co-author Mulukutla Sarma, *Northeastern University*, contributed to end-of-chapter multiple-choice questions and problems.

We commend the following Global Engineering team members at Cengage Learning: Timothy Anderson, Product Director; Mona ZefTel, Senior Content Developer; and Kristiina Paul, Freelance Permissions Researcher; as well as Rose Kernan of RPK Editorial Services, Inc. for their broad knowledge, skills, and ingenuity in publishing this edition. We also thank Jean Buttrom, Content Project Manager; Kristin Stine, Marketing Manager; Elizabeth Murphy, Engagement Specialist; Ashley Kaupert, Associate Media Content Developer; Teresa Versaggi and Alexander Sham, Product Assistants.

The reviewers for the sixth edition are as follows: Ross Baldick, *University of Texas at Austin*; François Bouffard, *McGill University*; Venkata Dinavahi, *University of Alberta*; Seyed Pouyan Jazayeri, *University of Calgary*; Bruno Osorno, *California State University at Northridge*; Zeb Tate, *University of Toronto*; and Mahyar Zarghami, *California State University at Sacramento*.

Substantial contributions to prior editions of this text were made by a number of invaluable reviewers, as follows:

- Fifth Edition: Thomas L. Baldwin, *Florida State University*; Ali Emadi, *Illinois Institute of Technology*; Reza Iravani, *University of Toronto*; Surya Santoso, *University of Texas at Austin*; Ali Shaban, *California Polytechnic State University, San Luis Obispo*; and Dennis O. Wiitanen, *Michigan Technological University*, and Hamid Jaffari, *Danvers Electric*.
- Fourth Edition: Robert C. Degeneff, *Rensselaer Polytechnic Institute*; Venkata Dina-vahi, *University of Alberta*; Richard G. Farmer, *Arizona State University*; Steven M. Hietpas, *South Dakota State University*; M. Hashem Nehrir, *Montana State University*; Anil Pahwa, *Kansas State University*; and Ghadir Radman, *Tennessee Technical University*.
- Third Edition: Sohrab Asgarpour, *University of Nebraska-Lincoln*; Mariesa L. Crow, *University of Missouri-Rolla*; Ilya Y. Grinberg, *State University of New York, College at Buffalo*; Iqbal Husain, *The University of Akron*; W. H. Kersting, *New Mexico State University*; John A. Palmer, *Colorado School of Mines*; Satish J. Ranada, *New Mexico State University*; and Shyama C. Tandon, *California Polytechnic State University*.
- Second Edition: Max D. Anderson, *University of Missouri-Rolla*; Sohrab Asgarpour, *University of Nebraska-Lincoln*; Kaveh Ashenayi, *University of Tulsa*; Richard D. Christie, Jr., *University of Washington*; Mariesa L. Crow, *University of Missouri-Rolla*; Richard G. Farmer, *Arizona State University*; Saul Goldberg, *California Polytechnic*

*University*; Clifford H. Grigg, *Rose-Hulman Institute of Technology*; Howard B. Hamilton, *University of Pittsburgh*; Leo Holzenthall, Jr., *University of New Orleans*; Walid Hubbi, *New Jersey Institute of Technology*; Charles W. Isherwood, *University of Massachusetts-Dartmouth*; W. H. Kersting, *New Mexico State University*; Wayne E. Knabach, *South Dakota State University*; Pierre-Jean Lagace, *IREQ Institut de Reserche a"Hydro-Quebec*; James T. Lancaster, *Alfred University*; Kwang Y. Lee, *Pennsylvania State University*; Mohsen Lotfalian, *University of Evansville*; Rene B. Marxheimer, *San Francisco State University*, Lamine Mili, *Virginia Polytechnic Institute and State University*; Osama A. Mohammed, *Florida International University*; Clifford C. Mosher, *Washington State University*, Anil Pahwa, *Kansas State University*; M. A. Pai, *University of Illinois at Urbana-Champaign*; R. Ramakumar, *Oklahoma State University*; Teodoro C. Robles, *Milwaukee School of Engineering*, Ronald G. Schultz, *Cleveland State University*; Stephen A. Sebo, *Ohio State University*; Raymond Shoults, *University of Texas at Arlington*, Richard D. Shultz, *University of Wisconsin at Platteville*; Charles Slivinsky, *University of Missouri-Columbia*; John P. Stahl, *Ohio Northern University*; E. K. Stanek, *University of Missouri-Rolla*; Robert D. Strattan, *University of Tulsa*; Tian-Shen Tang, *Texas A&M University-Kingsville*; S. S. Venkata, *University of Washington*; Francis M. Wells, *Vanderbilt University*; Bill Wieserman, *University of Pennsylvania-Johnstown*; Stephen Williams, *U.S. Naval Postgraduate School*; and Salah M. Yousif, *California State University-Sacramento*.

First Edition:

Frederick C. Brockhurst, *Rose-Hulman Institute of Technology*; Bell A. Cogbill, *Northeastern University*; Saul Goldberg, *California Polytechnic State University*; Mack Grady, *University of Texas at Austin*; Leonard F. Grigsby, *Auburn University*; Howard Hamilton, *University of Pittsburgh*; William F. Horton, *California Polytechnic State University*; W. H. Kersting, *New Mexico State University*; John Pavlat, *Iowa State University*; R. Ramakumar, *Oklahoma State University*; B. Don Russell, *Texas A&M*; Sheppard Salon, *Rensselaer Polytechnic Institute*; Stephen A. Sebo, *Ohio State University*; and Dennis O. Wiitanen, *Michigan Technological University*.

In conclusion, the objective in writing this text and the accompanying software package will have been fulfilled if the book is considered to be student-oriented, comprehensive, and up to date, with consistent notation and necessary detailed explanation at the level for which it is intended.

*J. Duncan Glover*

*Thomas J. Overbye*

*Mulukutla S. Sarma*

# List of Symbols, Units, and Notation

Symbol	Description	Symbol	Description
$a$	operator $1/120^\circ$	P	real power
$a_t$	transformer turns ratio	$q$	Charge
A	area	Q	reactive power
$A$	transmission line parameter	$r$	radius
$A$	symmetrical components transformation matrix	R	resistance
B	loss coefficient	R	turbine-governor regulation constant
B	frequency bias constant	<b>R</b>	resistance matrix
$B$	phasor magnetic flux density	$s$	Laplace operator
$B$	transmission line parameter	S	apparent power
C	capacitance	$S$	complex power
$C$	transmission line parameter	$t$	time
D	damping	T	period
D	distance	T	temperature
$D$	transmission line parameter	T	torque
$E$	phasor source voltage	$v(t)$	instantaneous voltage
$E$	phasor electric field strength	V	voltage magnitude (rms unless otherwise indicated)
$f$	frequency	$V$	phasor voltage
G	conductance	$V$	vector of phasor voltages
<b>G</b>	conductance matrix	X	reactance
H	normalized inertia constant	<b>X</b>	reactance matrix
$H$	phasor magnetic field intensity	Y	phasor admittance
$i(t)$	instantaneous current	<b>Y</b>	admittance matrix
I	current magnitude (rms unless otherwise indicated)	Z	phasor impedance
$I$	phasor current	<b>Z</b>	impedance matrix
<b>I</b>	vector of phasor currents	$\alpha$	angular acceleration
$j$	operator $1/90^\circ$	$\alpha$	transformer phase shift angle
J	moment of inertia	$\beta$	current angle
l	length		

Symbol	Description	Symbol	Description
$l$	length	$\beta$	area frequency response characteristic
$L$	inductance	$\delta$	voltage angle
$\mathbf{L}$	inductance matrix	$\delta$	torque angle
$N$	number (of buses, lines, turns, etc.)	$\varepsilon$	permittivity
p.f.	power factor	$\Gamma$	reflection or refraction coefficient
$p(t)$	instantaneous power	$\theta$	impedance angle
$\lambda$	magnetic flux linkage	$\theta$	angular position
$\lambda$	Penalty factor	$\mu$	permeability
$\Phi$	magnetic flux	$v$	velocity of propagation
$\rho$	resistivity	$\omega$	radian frequency
$\tau$	time in cycles		
$\tau$	transmission line transit time		

### SI Units

A	ampere
C	coulomb
F	farad
H	henry
Hz	hertz
J	joule
kg	kilogram
m	meter
N	newton
rad	radian
s	second
S	siemen
VA	voltampere
var	voltampere reactive
W	watt
Wb	weber
$\Omega$	ohm

### English Units

BTU	British thermal unit
Cmil	circular mil
ft	foot
hp	horsepower
in	inch
mi	mile

### Notation

Lowercase letters such as  $v(t)$  and  $i(t)$  indicate instantaneous values.

Uppercase letters such as  $V$  and  $I$  indicate rms values.

Uppercase letters in italic such as  $V$  and  $I$  indicate rms phasors.

Matrices and vectors with real components such as  $\mathbf{R}$  and  $\mathbf{I}$  are indicated by boldface type.

Matrices and vectors with complex components such as  $\mathbf{Z}$  and  $\mathbf{I}$  are indicated by boldface italic type.

Superscript T denotes vector or matrix transpose.

Asterisk (\*) denotes complex conjugate.

**PW** highlights problems that utilize PowerWorld Simulator.